





Radio Astronomy Synchrotron Emission

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Astronomy 423 at UNM Radio Astronomy

Radio Astronomy Notes - Synchrotron Emasion

relativistic és in a magnetic field

- 1) Lorentz transformations
- 2) Laws of nature are invariant in a moving france
- 3) The speed of light is the same in all frames

Consider frames & and &' with relative velocity v

$$X = \gamma \left(X' + v + v' \right)$$

$$Y = \gamma'$$

$$z = z'$$

$$x' = \gamma' \left(z' + v + v' \right)$$

$$+ = \gamma \left(+ \frac{\beta x'}{c} \right)$$

$$A = Y \left(T' + \beta X' \right) \qquad \beta = \frac{V}{C} \qquad Y = \frac{1}{V_{1-\beta^{2}}}$$





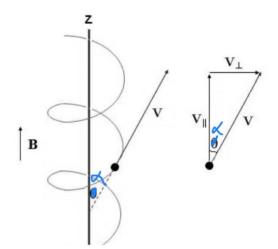
Synchrotron radiation of a single e in a constant Bfield

a = F/n $\frac{1}{1+} \left(\overrightarrow{Y} \overrightarrow{U} \right) = e \left(\overrightarrow{V} \times \overrightarrow{B} \right)$ It There is no \(\vec{E} = 0 \) then Energy conservation $V = constant \qquad V = constant$ Enry) dE = d (rmc2) = 0 Consider V1 and V1 $\frac{dV_{11}}{dt} = 0 \qquad \alpha_{1} = \frac{dV_{1}}{dt} = \frac{e}{rm} \left(V_{1} \times \vec{B} \right)$ V= TV12+V2 ... Vs must be constant as well





Radio Astronomy Notes - 2



the gyro frequency
$$V_G = \frac{W_G}{2\pi}$$

Total Power radiated: assume V1 = 0 for a dipole in frame &' P1 = 2 e q12 at relocity v dt= 8 dt/ P= dE E= rE' P= dE = dE dT' (Invariant under Corentt transform) = YdE', 1 = P' E= Ymec2 E= 8





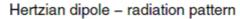
$$P = \frac{2e^{\gamma} V_{i}^{2} b^{2}}{3n^{2}c^{2}} \left(\frac{E}{mc^{2}}\right)^{2}$$

$$= 0_{7} \quad 7^{2}c \quad U_{B} \qquad 0_{7} = 6.65 \times 10^{-25} \text{cm}^{2}$$

$$fo \quad \text{stylk electron at velocity } V$$

$$\text{Lifetime estimate}$$

$$|r_{f}etime = \frac{1}{2} \quad \frac{E}{dE} = \frac{1}{2} \quad \frac{E}{p} = \frac{1}{2} \quad \frac{E}{16} \times \frac{1}{2} \quad \frac{E}{16} \times \frac{1}{2} = \frac{1}{2} \quad \frac{E}{16} \times \frac{1}{2} = \frac{1}{2} \cdot \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} = \frac{1}{2} \cdot \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} = \frac{1}{2}$$



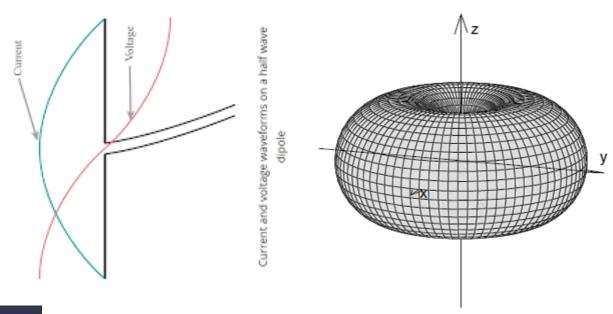


Figure 12.6 MATLAB plot of the 3-D normalized field polar radiation pattern of a Hertzian dipole (Fig.12.1); for MATLAB Exercise 12.17. (color figure on CW)

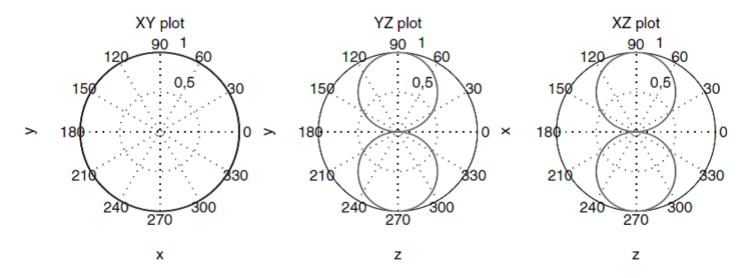


Figure 12.7 Cuts in three characteristic planes of the radiation pattern in Fig.12.6; for MATLAB Exercise 12.17. (color figure on CW)





-> in c frame Angular distribution: " Doppler Boostry " in observer's fame SMO = [5)no' [+ B cos 6' Friguracy Distribution Observer sees a pulse during angle & ~ f usry Popplar equation st = x (1-b) ot = 1 127 Short pulse => broad frequency = Two (sie RW 10.7.3)





Spectrum $\Gamma(v) = \sqrt{3} e^{3} \frac{0.5 \text{ m}}{\text{mc}^{2}} \propto \frac{v}{v_{c}} \int_{v_{c}}^{v_{c}} k_{5/5}(R) dR$ $\sqrt{c} = \frac{3}{2} r^{2} v_{c} \sin \alpha$ $= \frac{3}{2} r^{3} v_{b} \sin \alpha$ $\frac{v_{c}}{v_{c}} = \frac{3}{2} r^{3} v_{c} \sin \alpha$ $\frac{v_{c}}{v_{c}} = \frac{3}{2} r^{3} v_{c} \sin \alpha$

Example: B=10 mG what Y produces photons at S6He?
see worksheet

what is the Spectrum for an ensemble of rel. e.s.? $Ev = \int_{E} I(v) P(E) dE$





Worksheet #4

Download the worksheet from:

http://www.phys.unm.edu/~gbtaylor/astr423/WS4.pdf

Solve it in class.

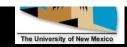
Ask questions if you are stuck

Tell me when you have the answer.





what is the Spectrum for an easeable of rel. e's? $\epsilon_{v} = \int_{E} I(v) P(E) dE$ N(E) dE= k E d E in astrophysies (powerlaw) $E_{\nu} = \int_{E_{\nu}}^{E_{\nu}} \rho(\gamma_{\nu_{e}}) \, t^{-s} \, dE$ $Ev = v^{\infty}$ where $\alpha = \frac{1}{2}(8-1)$ x = -0.75 s = -0.5



Polarization in a dayora field: $\frac{9}{1000} = \frac{-x+1}{-x+\frac{9}{3}} = 7270$ for x = -0.75in a random field: MIO

Every requirements: $w_{tot} = w_{part} + w_{nay} = v(u_p + u_b)$ $u_p = \eta + \int_{E_r}^{E_z} E^{1-\delta} dE \qquad \eta = filling factor$ $u_{nay} = \int_{exp}^{2} E = v_n c^2$

$$V_{L} = \frac{2}{\lambda} r^{2} v_{6} = \frac{3}{\lambda} \frac{eB}{m^{3}c^{5}} E^{2}$$

$$U_{p} = K \cdot G \cdot B^{\infty} - \frac{1}{\lambda} V_{2} + \alpha V_{2} +$$

next elemente & and solve for B when West is minimum

What $\frac{1}{8}$ $\frac{1}{8}$

Bre = (677-6-R2 SUV-X) 2/7

However thure is no guarantue that the System is at the minimum energy an alternative assumption is equipartition up = us



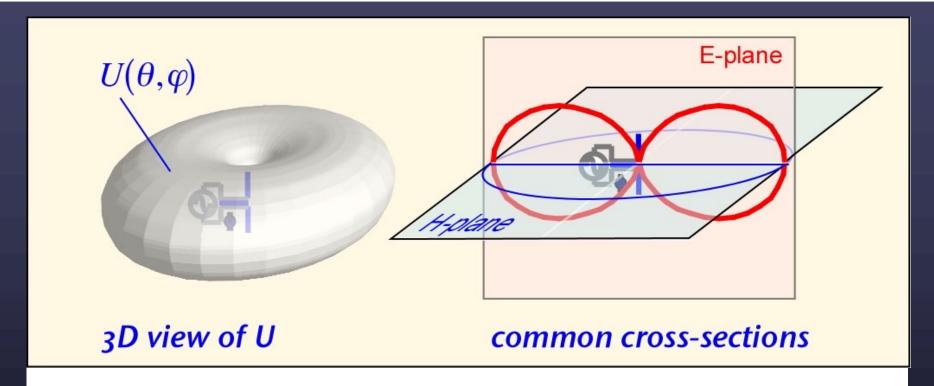


Synchrotron Self-absorption (55A): when energy density is high (To ~ Ten) VC= 3 82 VG ; KE = Themal E $V = \frac{1}{3k} = \frac{1}{3k} \left(\frac{v}{v_0} \right)^{1/2} \sim T_s$ $Sv = \frac{2kT_s}{s} = \frac{2m_s \Omega v^{5/2}}{3v_0 v_0} = \frac{2m_s \Omega v^{5/2}}{3v_0 v_0}$ SSA \\ \alpha \\ \frac{\text{0}^2 \nabla \frac{\text{5}}{\text{B}/\text{2}}}{\text{V}^{\text{\text{\text{\text{\text{optically thin}}}}} \\ \end{atom}





Hertz Dipole



 $A_e = G\lambda^2/4\pi$ G=1.5 for Hertz Dipole

G = 2.5 at 20 MHz for LWA

G = 4.0 at 60 MHz for LWA



