



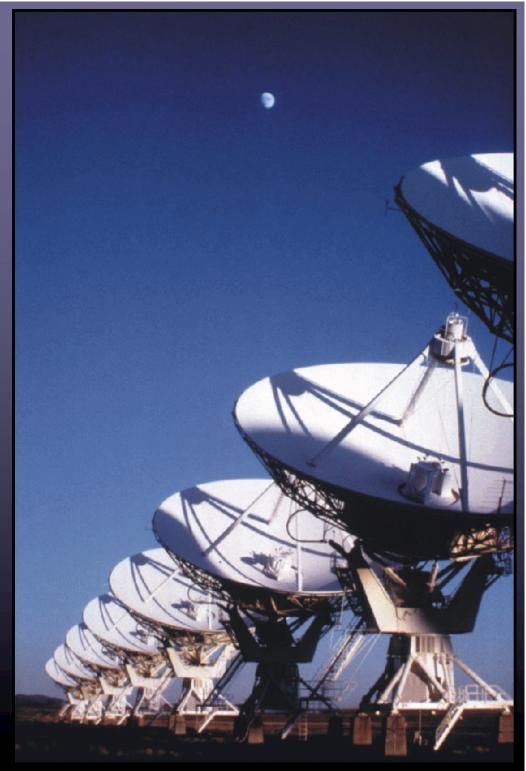




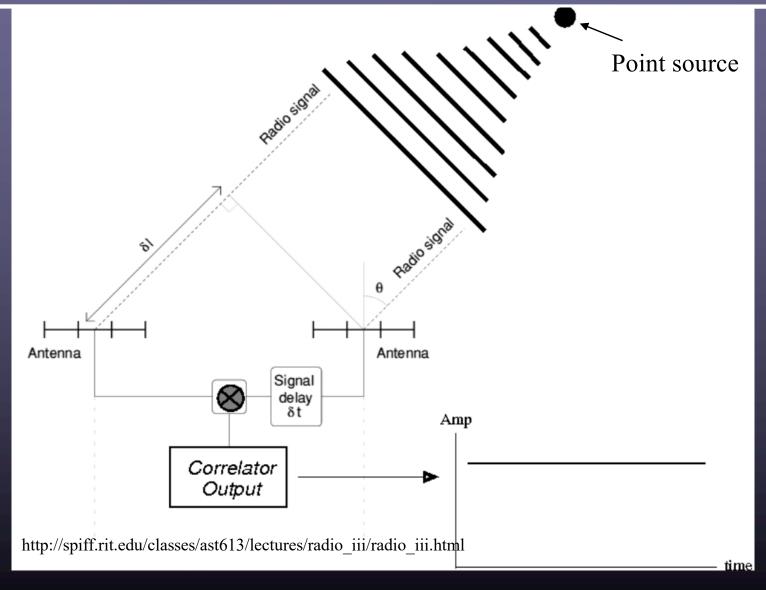
Calibration and Editing

Greg Taylor
University of New Mexico
Spring 2017

Astronomy 423 at UNM Radio Astronomy



Interferometry Basics



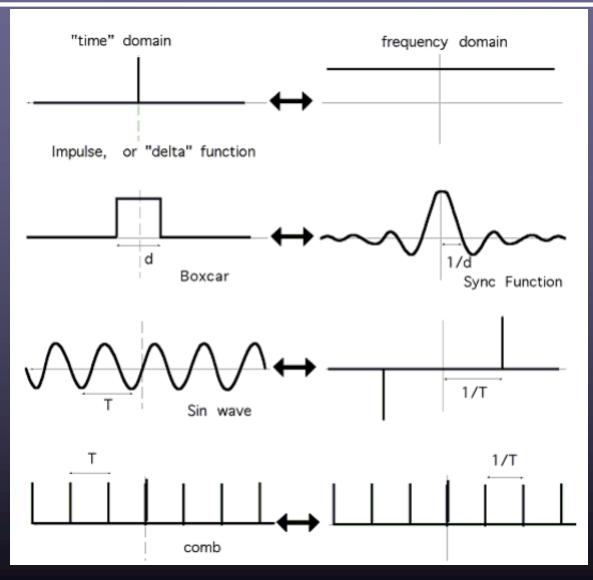




Fourier Transform Pairs

Name 3 FT relations: 1)AntennaAperture 2)

3)



Name 3 FT relations:

- 1) Power pattern
- 2)
- 3)

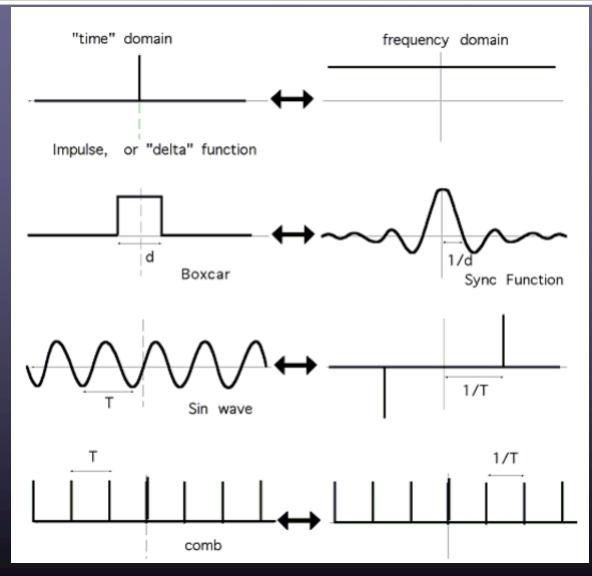




Fourier Transform Pairs

Name 3 FT relations:

- 1)AntennaAperture
- 2) Time series
- 3) Sky brightness



Name 3 FT relations:

- 1) Power pattern
- 2) Power spectrum
- 3) Visibility



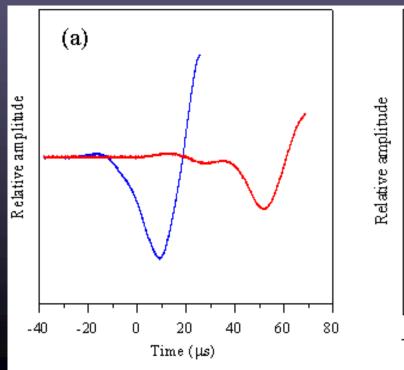


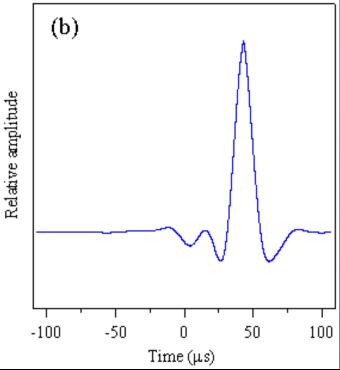
The Correlation Function

For continuous functions, f and g, the cross-correlation is defined as:

$$(f \star g)(t) \stackrel{\text{def}}{=} \int_{-\infty}^{\infty} f^*(\tau) g(t+\tau) d\tau,$$

where f * denotes the complex conjugate of f.







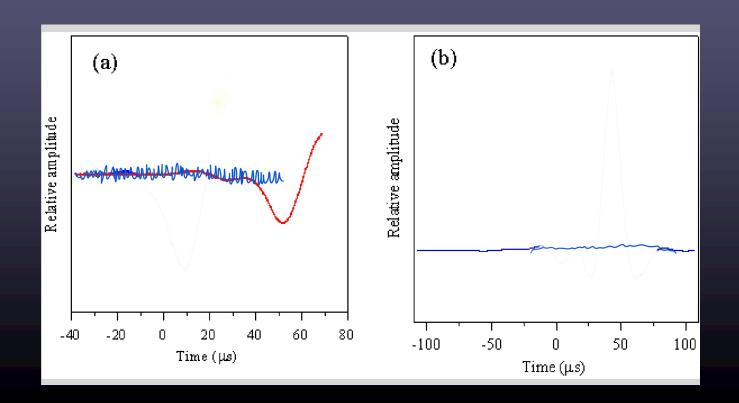


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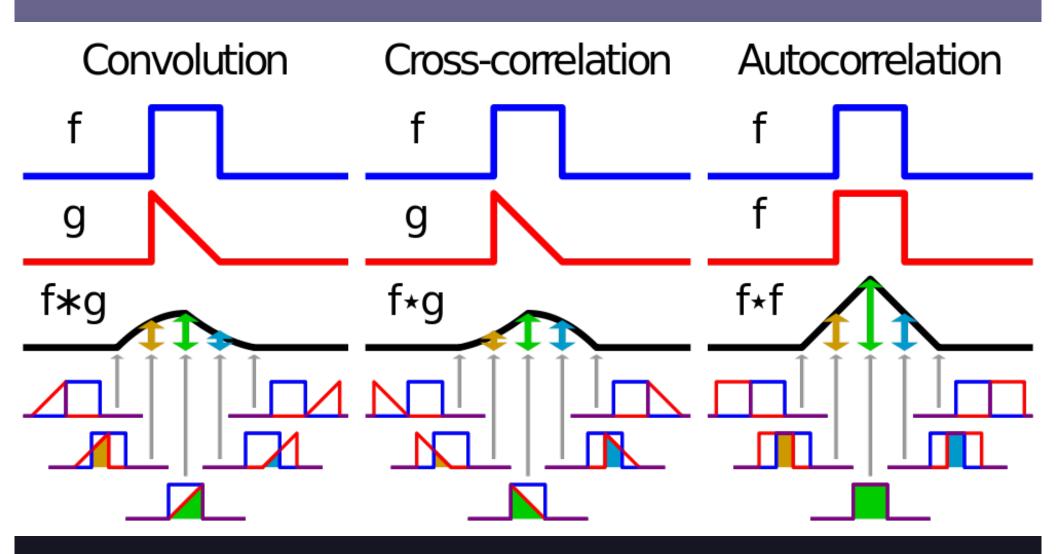
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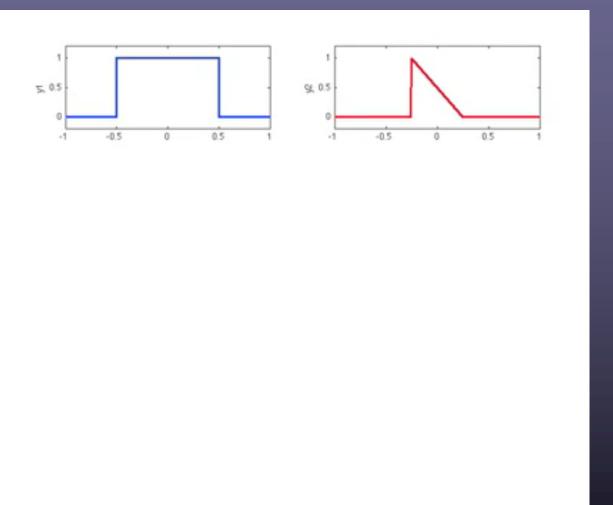












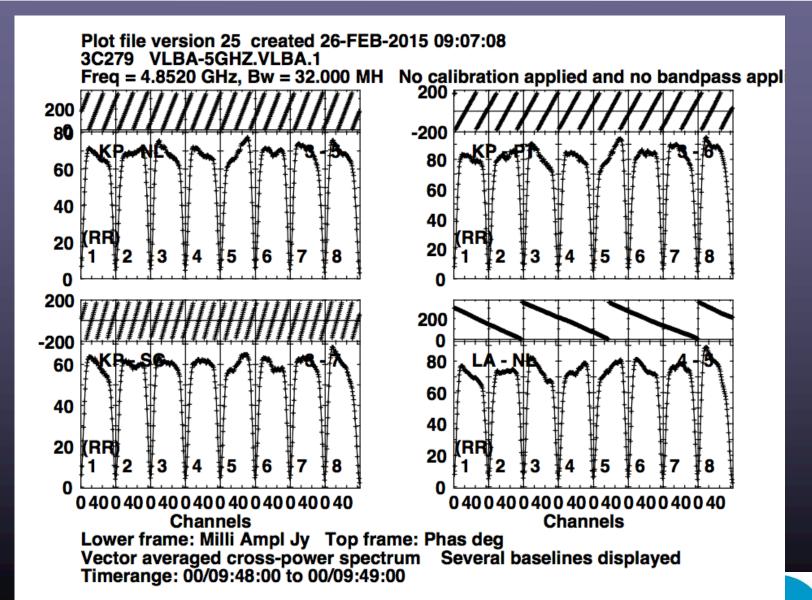




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Fringe Fitting

2015 ASTR423 VLBA obs 3C279





Announcements

- HW4 12 received, 1 MIA
- VLA observing done!
- LWA observing?
- Exam 1 on Wednesday, March 3
- Constants posted
- Review problem 3-1
- Send me your choices





Outline

- Why calibrate and edit?
- How to calibrate
- What to Edit
- Practical Calibration Planning
- Calibration Evaluation
- A Dictionary of Calibration Components
- More on editing and RFI
- Summary

This lecture is complementary to Chapter 5 of ASP 180 and is based on a lecture by George Moellenbrock





Why Calibration and Editing?

- Synthesis radio telescopes, though well-designed, are not perfect (e.g., surface accuracy, receiver noise, polarization purity, stability, etc.)
- Need to accommodate engineering (e.g., frequency conversion, digital electronics, etc.)
- Hardware or control software occasionally fails or behaves unpredictably
- Scheduling/observation errors sometimes occur (e.g., wrong source positions)
- Atmospheric conditions not ideal (not limited to "bad" weather)
- Radio Frequency Interference (RFI)

Determining *instrumental properties* (calibration) is as important as determining *radio source properties*





From Idealistic to Realistic

 Formally, we wish to obtain the visibility function, which we intend to invert to obtain an image of the sky:

$$V(u,v) = \int_{sky} I(l,m)e^{-i2\pi(ul+vm)}dl \ dm$$

- In practice, we correlate (multiply & average) the electric field (voltage) samples, x_i & x_j , received at pairs of telescopes (i,j)
 - Averaging duration is set by the expected timescales for variation of the correlation result (typically 10s or less for the VLA)
- Single radio telescopes are devices for collecting the signal $x_i(t)$ and providing it to the correlator.





What signal is really collected?

• The net signal delivered by antenna i, $x_i(t)$, is a combination of the desired signal, $s_i(t,l,m)$, corrupted by a factor $J_i(t,l,m)$ and integrated over the sky, and noise, $n_i(t)$:

$$x_i(t) = \int_{sky} J_i(t, l, m) s_i(t, l, m) dldm + n_i(t)$$
$$= s'_i(t) + n_i(t)$$

- $J_i(t,l,m)$ is the product of a host of effects which we must calibrate
- In some cases, effects implicit in the $J_i(t,l,m)$ term corrupt the signal irreversibly and the resulting data must be *edited*
- $J_i(t,l,m)$ is a complex number
- J_i(t,l,m) is antenna-based
- Usually, $|n_i| >> |s_i|$





The Measurement Equation

 We can now write down the calibration situation in a general way - the Measurement Equation:

$$\vec{V}_{ij}^{obs} = \int_{sky} (\vec{J}_i \otimes \vec{J}_j^*) \vec{I}(l,m) e^{-i2\pi(u_{ij}l + v_{ij}m)} dldm$$

…and consider how to solve it!





The Measurement Equation - Simplified

$$\vec{V}_{ij}^{obs} = \int_{sky} (\vec{J}_i \otimes \vec{J}_j^*) \vec{I}(l,m) e^{-i2\pi(u_{ij}l + v_{ij}m)} dldm$$

First, is olate non-direction-dependent effects, and factor them from the integral:

$$= \left(\vec{J}_{i}^{vis} \otimes \vec{J}_{j}^{vis*}\right) \int_{skv} \left(\vec{J}_{i}^{sky} \otimes \vec{J}_{j}^{sky*}\right) \vec{I} (l,m) e^{-i2\pi \left(u_{ij}l + v_{ij}m\right)} dldm$$

Next, we recognize that it is often possible to assume $J^{sky}=1$, and we have a relationship between ideal and observed Visibilities:

$$= \left(\vec{J}_{i}^{vis} \otimes \vec{J}_{j}^{vis*}\right) \int_{sky} \vec{I}(l,m) e^{-i2\pi \left(u_{ij}l + v_{ij}m\right)} dldm$$

$$\vec{V}_{ij}^{obs} = \left(\vec{J}_{i}^{vis} \otimes \vec{J}_{j}^{vis*}\right) \vec{V}_{ij}^{ideal}$$

$$\vec{V}_{ij}^{obs} = \left(\vec{J}_i^{vis} \otimes \vec{J}_j^{vis*}\right) \vec{V}_{ij}^{ideal}$$





Solving the Measurement Equation

 The J terms can be factored into a series of components representing physical elements along the signal path:

$$\vec{V}_{ij}^{obs} = \left(\vec{J}_i^1 \otimes \vec{J}_j^{1*}\right) \left(\vec{J}_i^2 \otimes \vec{J}_j^{2*}\right) \left(\vec{J}_i^3 \otimes \vec{J}_j^{3*}\right) \left(\vec{J}_i^{...} \otimes \vec{J}_j^{...*}\right) \vec{V}_{ij}^{ideal}$$

 Depending upon availability of estimates for various J terms, we can re-arrange the equation and solve for any single term, if we know V^{ideal}:

$$\left[\left(\vec{J}_{i}^{2} \otimes \vec{J}_{j}^{2*} \right)^{-1} \left(\vec{J}_{i}^{1} \otimes \vec{J}_{j}^{1*} \right)^{-1} \vec{V}_{ij}^{obs} \right] = \left(\vec{J}_{i}^{solve} \otimes \vec{J}_{j}^{solve*} \right) \left[\left(\vec{J}_{i}^{4} \otimes \vec{J}_{j}^{4*} \right) \left(\vec{J}_{i}^{...} \otimes \vec{J}_{j}^{...*} \right) \vec{V}_{ij}^{ideal} \right]$$

After obtaining estimates for all relevant J, data can be corrected:

$$\vec{V}_{ij}^{corrected} = \left(\vec{J}_i^{...} \otimes \vec{J}_j^{...*}\right)^{-1} \left(\vec{J}_i^3 \otimes \vec{J}_j^{3*}\right)^{-1} \left(\vec{J}_i^2 \otimes \vec{J}_j^{2*}\right)^{-1} \left(\vec{J}_i^1 \otimes \vec{J}_j^{1*}\right)^{-1} \vec{V}_{ij}^{obs}$$





Solving the Measurement Equation

 Formally, solving for any calibration component is always the same non-linear fitting problem:

$$ec{V}_{ij}^{corrected \cdot obs} = \left(ec{J}_{i}^{solve} \otimes ec{J}_{j}^{solve*}
ight) ec{V}_{ij}^{corrupted \cdot ideal}$$

- Algebraic particulars are stored safely and conveniently inside the matrix formalism (out of sight, out of mind!)
- Viability of the solution depends on the underlying algebra (hardwired in calibration applications) and relies on *proper* calibration observations





Antenna-based Calibration

- Success of synthesis telescopes relies on antenna-based calibration
 - N antenna-based factors, N(N-1) visibility measurements
 - Fundamentally, only information that cannot be factored into antennabased terms is believable as being of astronomical origin
- Closure: calibration-independent observables:
 - Closure phase (3 baselines):

$$\begin{aligned} \phi_{ij}^{obs} + \phi_{jk}^{obs} + \phi_{ki}^{obs} &= \phi_{ij}^{real} + (\theta_i - \theta_j) + \phi_{jk}^{real} + (\theta_j - \theta_k) + \phi_{ki}^{real} + (\theta_k - \theta_i) \\ &= \phi_{ij}^{real} + \phi_{jk}^{real} + \phi_{ki}^{real} \end{aligned}$$

• Closure amplitude (4 baselines):

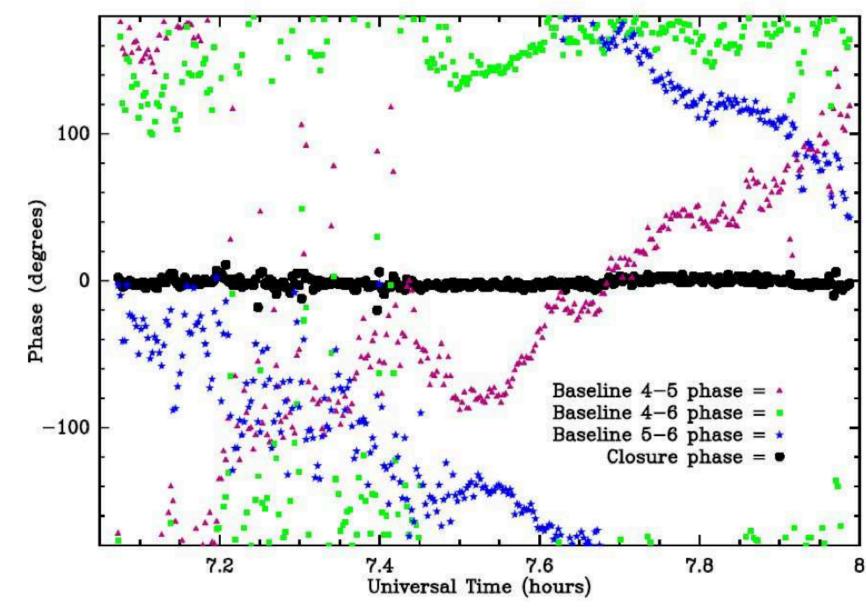
$$\begin{vmatrix} V_{ij}^{obs} V_{kl}^{obs} \\ V_{ik}^{obs} V_{jl}^{obs} \end{vmatrix} = \begin{vmatrix} J_{i} J_{j} V_{ij}^{real} J_{k} J_{l} V_{kl}^{real} \\ J_{i} J_{k} V_{ik}^{real} J_{j} J_{l} V_{jl}^{real} \end{vmatrix}$$
$$= \begin{vmatrix} V_{ij}^{real} V_{kl}^{real} \\ V_{ik}^{real} V_{jl}^{real} \end{vmatrix}$$





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Antenna-based Calibration





Planning for Good Calibration

- A priori calibrations (provided by the observatory)
 - Antenna positions, earth orientation and rate
 - Clocks
 - Antenna pointing, gain, voltage pattern
 - Calibrator coordinates, flux densities, polarization properties
- Absolute flux calibration
 - True calibration very difficult, requires great effort
 - Substitute is to reference to a source of known flux (e.g., 3C286)
- Cross-calibration
 - Observe nearby point sources against which calibration components can be solved, and transfer solutions to target observations
 - Choose appropriate calibrators for different components; usually strong point sources because we can predict their visibilities
 - Choose appropriate timescales for each component
- Simple (common) example, Gain and Bandpass:

$$\vec{V}_{ij}^{obs} = \left(\vec{B}_{i} \otimes \vec{B}_{j}^{*}\right) \left(\vec{G}_{i} \otimes \vec{G}_{j}^{*}\right) \vec{V}_{ij}^{ideal}$$
$$= \vec{B}_{ij} \vec{G}_{ij} \vec{V}_{ij}^{ideal}$$





"Electronic" Gain, G

- Catch-all for most amplitude and phase effects introduced by antenna electronics (amplifiers, mixers, quantizers, digitizers)
 - Most commonly treated calibration component
 - Dominates other effects for standard VLA observations
 - Includes scaling from engineering (correlation coefficient) to radio astronomy units (Jy), by scaling solution amplitudes according to observations of a flux density calibrator
 - Often also includes ionospheric and tropospheric effects which are typically difficult to separate unto themselves





Bandpass Response, B

- *G*-like component describing frequency-dependence of antenna electronics, etc.
 - Filters used to select frequency passband not square
 - Optical and electronic reflections introduce ripples across band
 - Often assumed time-independent, but not necessarily so
 - Typically (but not necessarily) normalized





Hello, Dr

Total Time

00:00:09.945

00:00:39.945

00:04:00.000

00:01:34.643

00:01:34.287

124.4d 2

118.5d 1

125.5d 00:01:24.954

Typical VLA observation



CalGain

ObsTat

19h 27m 48.49520s --- ---

--- ---

73d 58' 1.5700"

19h 8m 23.385s

2.5GHz

3.5GHz

2.5GHz

2.96

3.03

3.30



🗓 🚺 (1X) AFGL Ku and C 😐 🚺 (4X) AFGL Ku Band

R STD: Phase cal Ku

🗎 🚺 (1X) 4C 19.71 S and

🖮 🚺 (1X) WISE S and C E

J1927+7358

4C +72.26

J2000

Phase cal S

(3) S16f2A

4C +72.26

Uncalibrated spectra on 3C286

Plot file version 2 created 07-MAR-2011 07:58:58 **MULTI.UVDATA.1** Freq = 22.5240 GHz, Bw = 128.000 MH No calibration applied and no bandpass applied 70 220 50 30 180 20 W36 - N24 W36 - E32 8 8 6 -{IF 1(RR) IF 2(RR) IF 2(RR) 200 30 10 100 W36 - N28 8 4 5 IF 1(RR) IF 2(RR) IF 1(RR) 0 180 200 -95 140 100 105 100 W36 - N32 8 8 5 4 IF 2(RR) IF 1(RR) IF 2(RR) 0 20 40 60 20 40 60 20 40 60 Channels Channels Channels Lower frame: Milli Ampl Jy Top frame: Phas deg

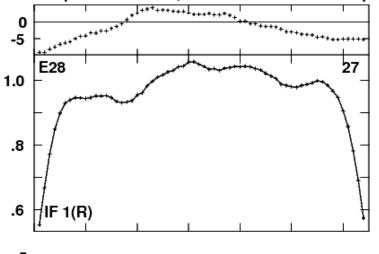
Scalar averaged cross-power spectrum Several baselines displayed

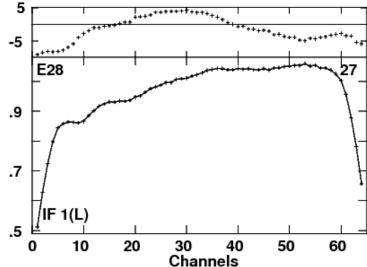
Timerange: 00/14:06:00 to 00/14:07:00



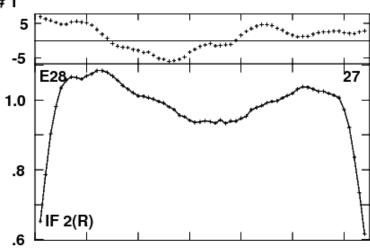
Bandpass solutions

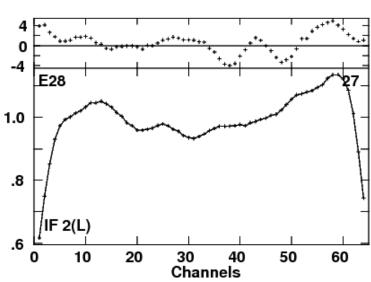
Plot file version 48 created 07-MAR-2011 08:07:20 MULTI.UVDATA.1 Freq = 22.3960 GHz, Bw = 128.000 MH Bandpass table # 1





Lower frame: BP ampl Top frame: BP phase Bandpass table spectrum Antenna: * Timerange: 00/14:01:08 to 00/14:04:08



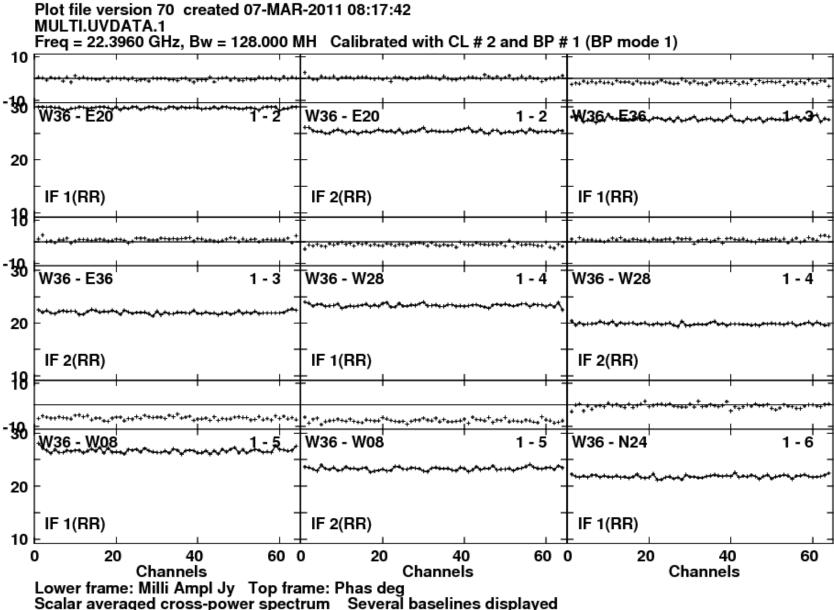






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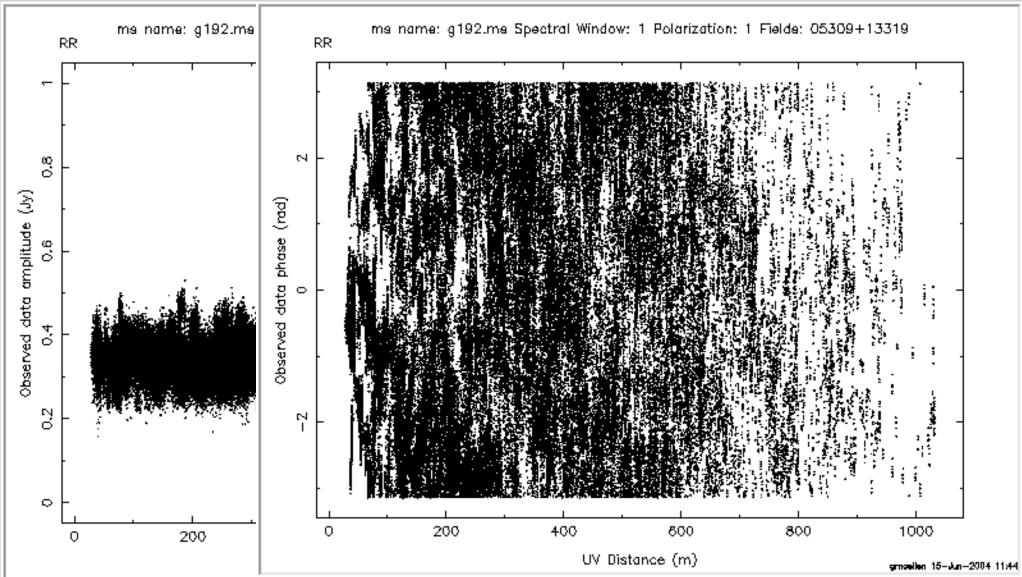
Spectra after Fringe-fit and bandpass calibration





Timerange: 00/14:02:01 to 00/14:04:01

Observed Data vs. UV dist

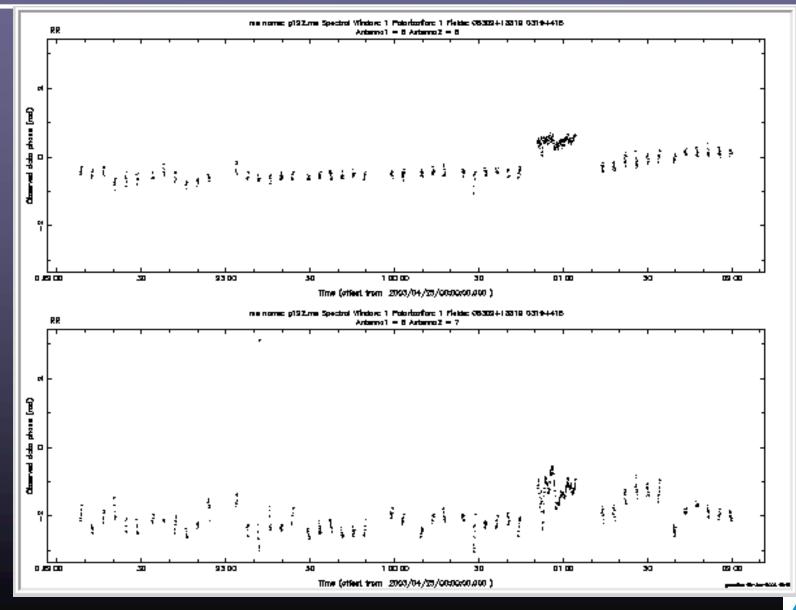






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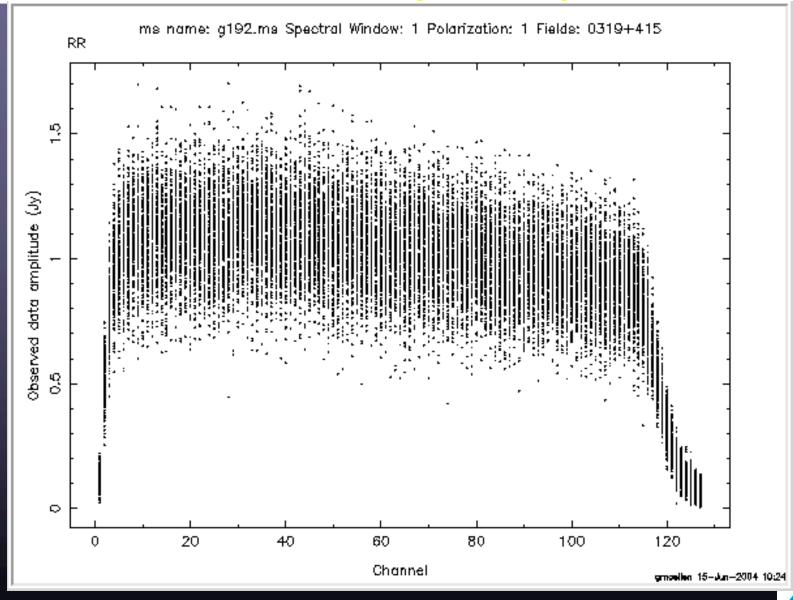
Observed Data – Phase vs. Time





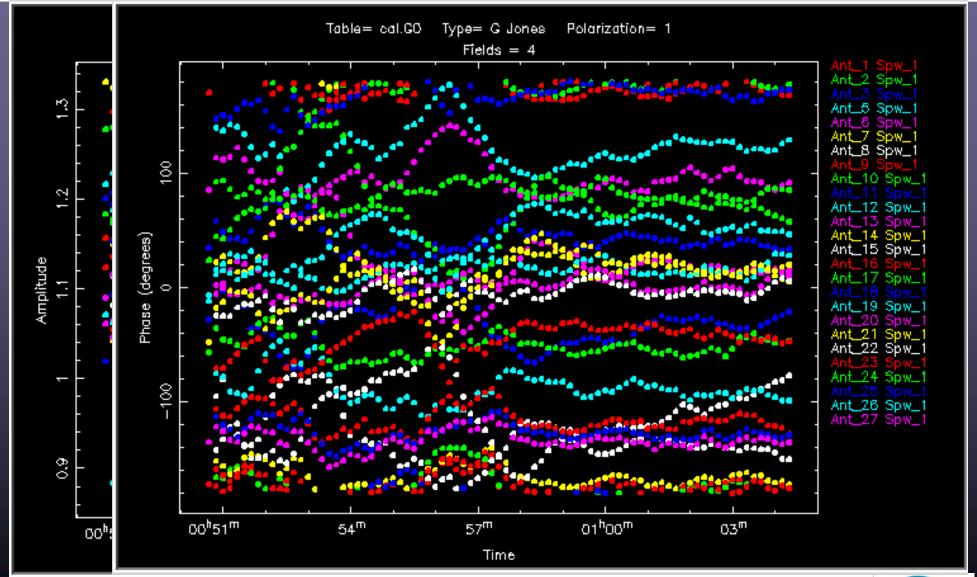
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Observed Data – Amplitude Spectrum





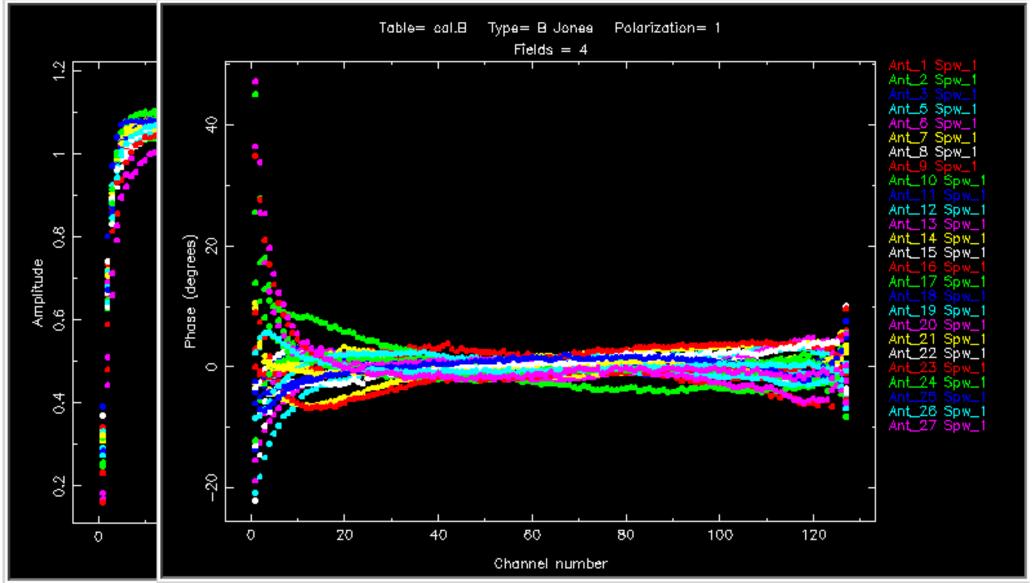
Gain Amp/Phase Solutions (B calibrator)







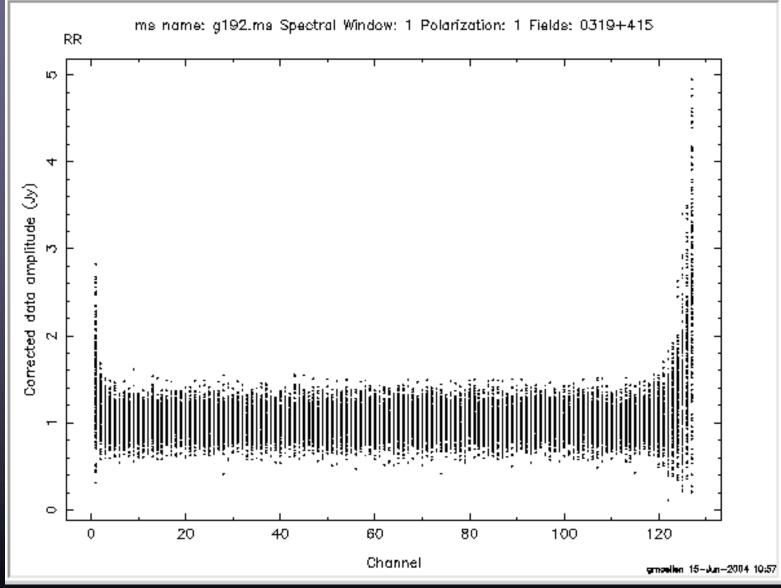
Bandpass Solutions







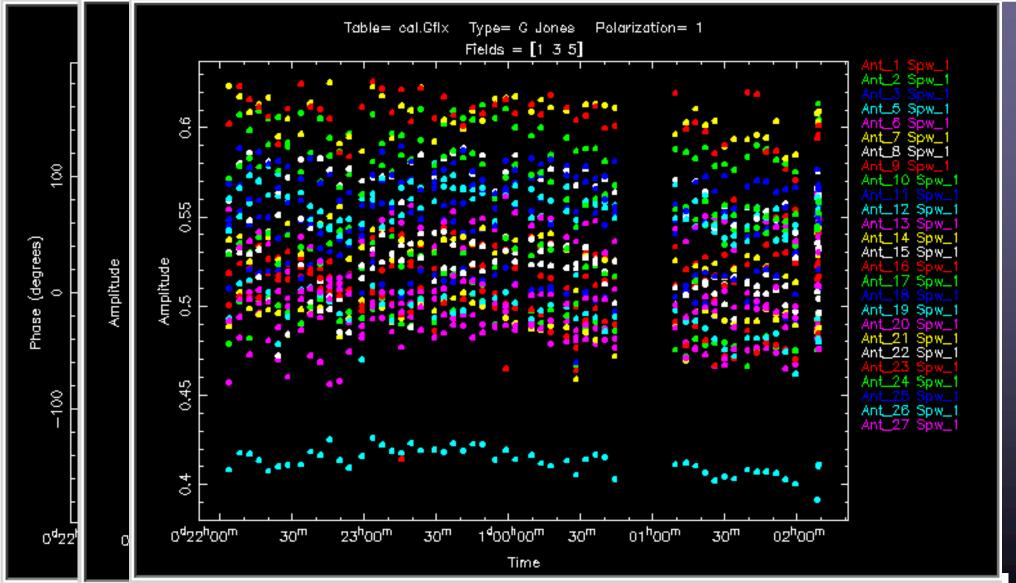
Bandpass-Calibrated Data (Amplitude)







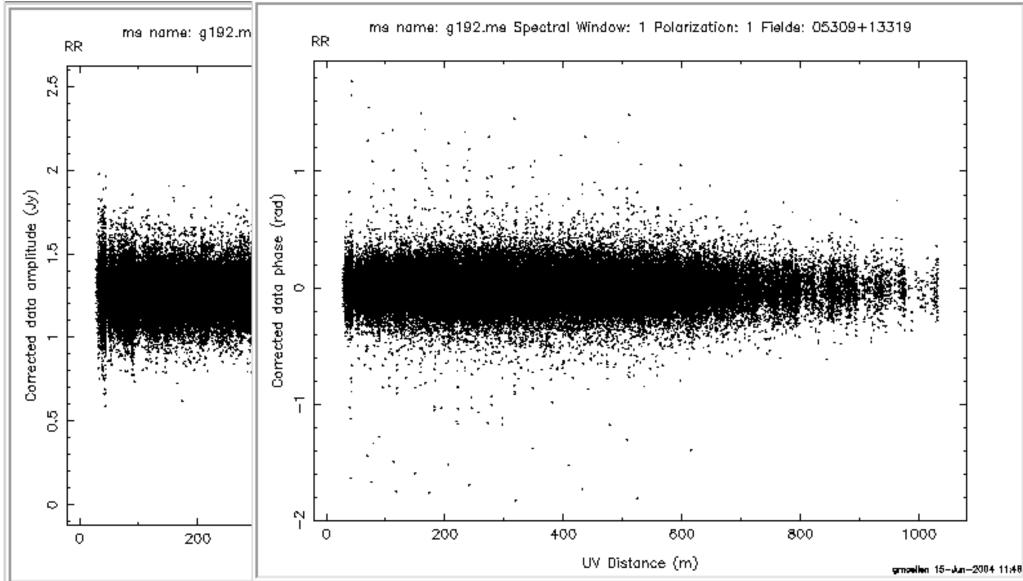
Gain Amp/Phase Solutions







Corrected Data vs. UV dist

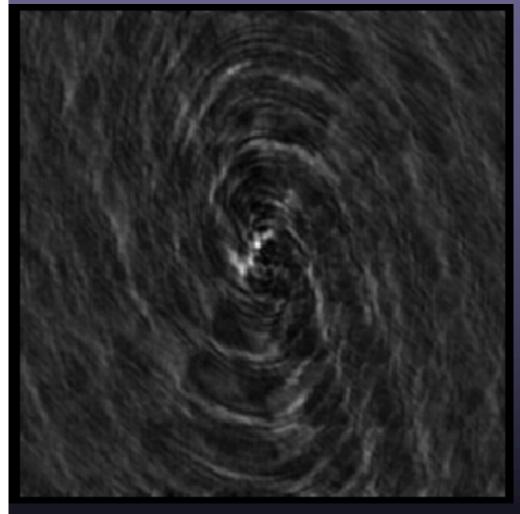


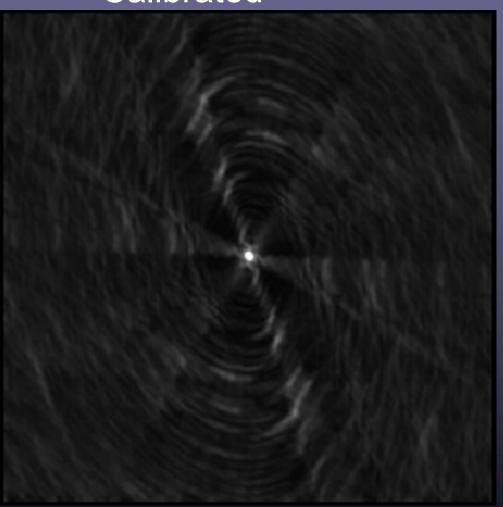




Effect of Calibration in the Image Plane

Uncalibrated Calibrated









A Dictionary of Calibration Components

- J_i contains many components:
 - *F* = ionospheric Faraday rotation
 - T = tropospheric effects
 - P = parallactic angle
- $\vec{J}_i = \vec{K}_i \vec{B}_i \vec{G}_i \vec{D}_i \vec{E}_i \vec{P}_i \vec{T}_i \vec{F}_i$
- *E* = antenna voltage pattern
- *D* = polarization leakage
- *G* = electronic gain
- B = bandpass response
- *K* = geometric compensation
- Order of terms follows signal path (right to left)
- Direction-dependent terms involve FT in solution





Tropospheric Effects, T

- The troposphere causes polarization-independent amplitude and phase effects due to emission/opacity and refraction, respectively
 - Typically 2-3m excess path length at zenith compared to vacuum
 - Higher noise contribution, less signal transmission: Lower SNR
 - Most important at v > 15 GHz where water vapor absorbs/emits
 - More important nearer horizon where tropospheric path length greater
 - Clouds, weather = variability in phase and opacity; may vary across array
 - Water vapor radiometry? Phase transfer from low to high frequencies?





Parallactic Angle, P

- Orientation of sky in telescope's field of view
 - Constant for equatorial telescopes
 - Varies for alt-az-mounted telescopes:

$$\chi(t) = \arctan\left(\frac{\cos(l)\sin(h(t))}{\sin(l)\cos(\delta) - \cos(l)\sin(\delta)\cos(h(t))}\right)$$

$$l = \text{latitude}, \ h(t) = \text{hour angle}, \ \delta = \text{declination}$$

- Rotates the position angle of linearly polarized radiation
- Analytically known, and its variation provides leverage for determining polarization-dependent effects





Antenna Voltage Pattern, E

- Antennas of all designs have direction-dependent gain
 - Important when region of interest on sky comparable to or larger than λ/D
 - Important at lower frequencies where radio source surface density is greater and wide-field imaging techniques required
 - Beam squint: E^p and E^q not parallel, yielding spurious polarization
 - For convenience, direction dependence of polarization leakage (D)
 may be included in E (off-diagonal terms then non-zero)





Polarization Leakage, D

- Polarizer is not ideal, so orthogonal polarizations not perfectly isolated
 - Well-designed feeds have D ~ a few percent or less
 - A geometric property of the feed design, so frequency dependent
 - For *R*,*L* systems, total-intensity imaging affected as ~*DQ*, *DU*, so only important at high dynamic range (*Q*,*U*~*D*~*few* %, typically)
 - For R,L systems, linear polarization imaging affected as ~DI, so almost always important





"Electronic" Gain, G

- Catch-all for most amplitude and phase effects introduced by antenna electronics (amplifiers, mixers, quantizers, digitizers)
 - Most commonly treated calibration component
 - Dominates other effects for standard VLA observations
 - Includes scaling from engineering (correlation coefficient) to radio astronomy units (Jy), by scaling solution amplitudes according to observations of a flux density calibrator
 - Often also includes ionospheric and tropospheric effects which are typically difficult to separate unto themselves
 - Excludes frequency dependent effects





Bandpass Response, B

- *G*-like component describing frequency-dependence of antenna electronics, etc.
 - Filters used to select frequency passband not square
 - Optical and electronic reflections introduce ripples across band
 - Often assumed time-independent, but not necessarily so
 - Typically (but not necessarily) normalized





Geometric Compensation, K

- Must get geometry right for Synthesis Fourier Transform relation to work in real time; residual errors here require "Fringe-fitting"
 - Antenna positions (geodesy)
 - Source directions (time-dependent in topocenter!) (astrometry)
 - Clocks
 - Electronic pathlengths
 - Importance scales with frequency and baseline length





Non-closing Effects:

- Correlator-based errors which do not decompose into antenna-based components
 - Most digital correlators designed to limit such effects to well-understood and uniform scaling laws (absorbed in G)
 - Additional errors can result from averaging in time and frequency over variation in antenna-based effects and visibilities (practical instruments are finite!)
 - RFI
 - Virtually indistinguishable from source structure effects
 - Geodetic observers consider determination of radio source structure—a baseline-based effect—as a required calibration if antenna positions are to be determined accurately





Calibrator Rules of Thumb

- T, G, K:
 - Strong and point-like sources, as near to target source as possible
 - Observe often enough to track phase and amplitude variations: calibration intervals of up to 10s of minutes at low frequencies (beware of ionosphere!), as short as 1 minute or less at high frequencies
 - Observe at least one calibrator of known flux density at least once
- B:
- Strong enough for good sensitivity in each channel (often, *T*, *G* calibrator is ok), point-like if visibility might change across band
- Observe often enough to track variations (e.g., waveguide reflections change with temperature and are thus a function of time-of-day)
- D:
- Best calibrator for full calibration is strong and pointlike
- If polarized, observe over a broad range of parallactic angle to disentangle *D*s and source polarization (often, *T*, *G* calibrator is ok)
- F:
- Choose strongly polarized source and observe often enough to track variation





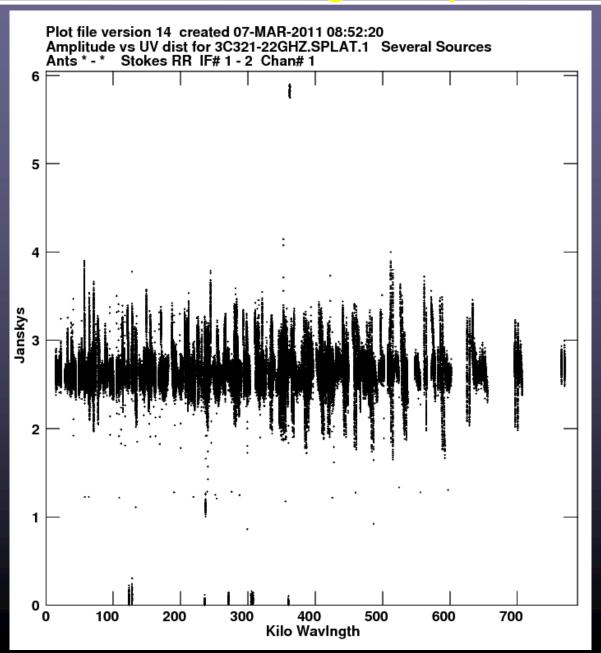
Data Examination and Editing

- After observation, initial data examination and editing very important
 - Will observations meet goals for calibration and science requirements?
 - Some real-time flagging occurred during observation (antennas off-source, LO out-of-lock, etc.). Any such bad data left over? (check operator's logs)
 - Any persistently 'dead' antennas (J_i =0 during otherwise normal observing)? (look at data on strong calibrators)
 - Amplitude and phase should be continuously varying—edit outliers
 - Any antennas shadowing others? Edit such data.
 - Be conservative: those antennas/timeranges which are bad on calibrators are probably bad on weak target sources—edit them
 - Periods of poor weather? (check operator's log)
 - Distinguish between bad (hopeless) data and poorly-calibrated data.
 E.g., some antennas may have significantly different amplitude response which may not be fatal—it may only need to be calibrated
 - Radio Frequency Interference (RFI)?
 - Choose reference antenna wisely (ever-present, stable response)





A Data Editing Example







Radio Frequency Interference

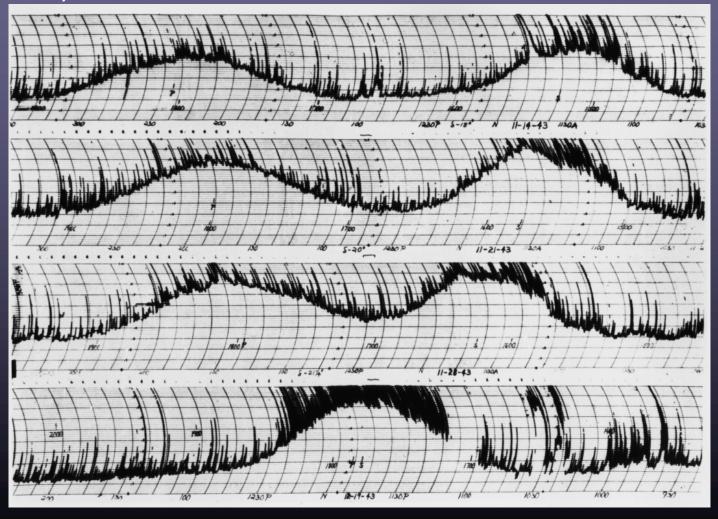
- RFI originates from man-made signals generated in the antenna electronics or by external sources (e.g., satellites, cell-phones, radio and TV stations, automobile ignitions, microwave ovens, etc.)
 - Adds to total noise power in all observations, thus decreasing sensitivity to desired natural signal, possibly pushing electronics into non-linear regimes
 - As a contribution to the n_i term, can correlate between antennas if of common origin and baseline short enough (insufficient decorrelation via geometric delay)
 - When RFI is correlated, it obscures natural emission in spectral line observations





Radio Frequency Interference

 Has always been a problem (Reber, 1944, in total power)!

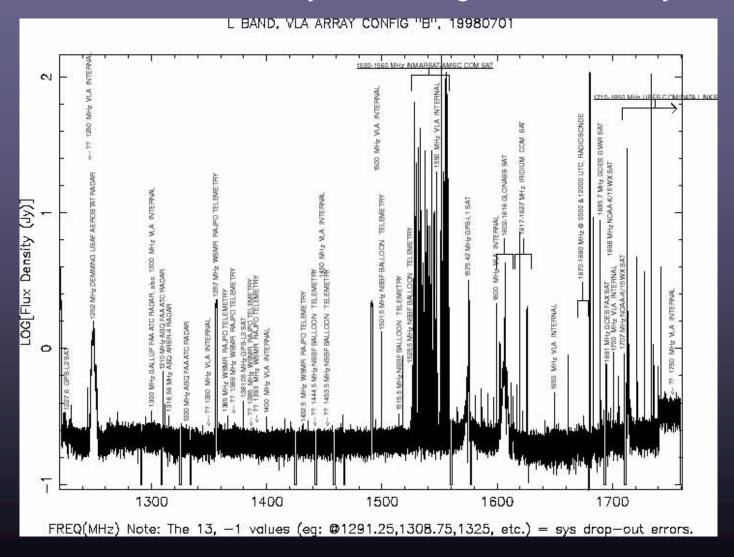






Radio Frequency Interference (cont)

Growth of telecom industry threatening radioastronomy!







Radio Frequency Interference (cont)

- RFI Mitigation
 - Careful electronics design in antennas, including notch filters
 - High-dynamic range digital sampling
 - Observatories world-wide lobbying for spectrum management
 - Choose interference-free frequencies (or at least be prepared to throw away lots of bandwidth – VLA 1-2 GHz only ~500 MHz useful)
 - Observe continuum experiments in spectral-line modes so affected channels can be edited
- Various off-line mitigation techniques under study





Summary

- Determining calibration is as important as determining source structure—can't have one without the other
- Calibration dominated by antenna-based effects, permits separation of calibration from astronomical information
- Calibration determination is a single standard fitting problem
- Calibration an iterative process, improving various components in turn
- Strong point sources are the best calibrators
- Observe calibrators according requirements of components
- Data examination and editing an important part of calibration





Further Reading

- http://www.nrao.edu/whatisra/mechanisms.shtml
- http://www.nrao.edu/whatisra/
- www.nrao.edu
- Synthesis Imaging in Radio Astronomy
- ASP Vol 180, eds Taylor, Carilli & Perley



